

# Study on Crack Patterns of a Reinforced Building

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## Abstract

The present work results from the observation of some crack patterns, which occurred in several construction elements of a reinforced concrete building located in the Sakurajima area.

The following two studies were made:

(I)-The crack patterns produced in the largest slab of second floor.

The causes of the cracks in the slab were analyzed on the basis of four specific considerations of Japanese method of calculation (AIJ:Architectural Institute of Japan) and of German method of calculation (DIN), for reinforced concrete buildings:

- (a)-The thickness of the slab.
- (b)-A determination of the required area of steel, which was calculated from the bending moment of the slab.
- (c)-A comparison between the calculated fiber tensile stress of the concrete and the allowable tensile stress of concrete.
- (d)-Bond stress and shear stress.

(II)-The crack patterns were caused by a differential subsidence of some foundation components.

## RESUMEN

El presente trabajo ha sido realizado a partir de la observación de la fisuración producida en diferentes elementos constructivos de un edificio construido en hormigón armado ubicado en el área del Sakurashima.

Los siguientes dos estudios fueron realizados:

(I) La fisuración producida en la mayor losa perteneciente al segundo piso.

Las causas de la fisuración de la losa fueron analizadas en base a cuatro específicas consideraciones del método de cálculo japones (AIJ, Instituto de Arquitectura del Japón) y de acuerdo al método de cálculo alemán (DIN), para edificios de hormigón armado:

- (a) El espesor de la losa.
- (b) Determinación de la cuantía de acero necesaria, la que fue calculada a partir de los momentos fléctores de la losa.
- (c) Comparación entre los valores de la resistencia a la tracción del hormigón asumido como

real y la resistencia admisible a la tracción del hormigón.

(d) Tensión de adherencia entre el hormigón y el acero; tensión de corte del hormigón.

- (II) La fisuración originada a partir del descenso diferencial entre algunos componentes de la fundación del edificio.

PHOTO Exterior View of Building



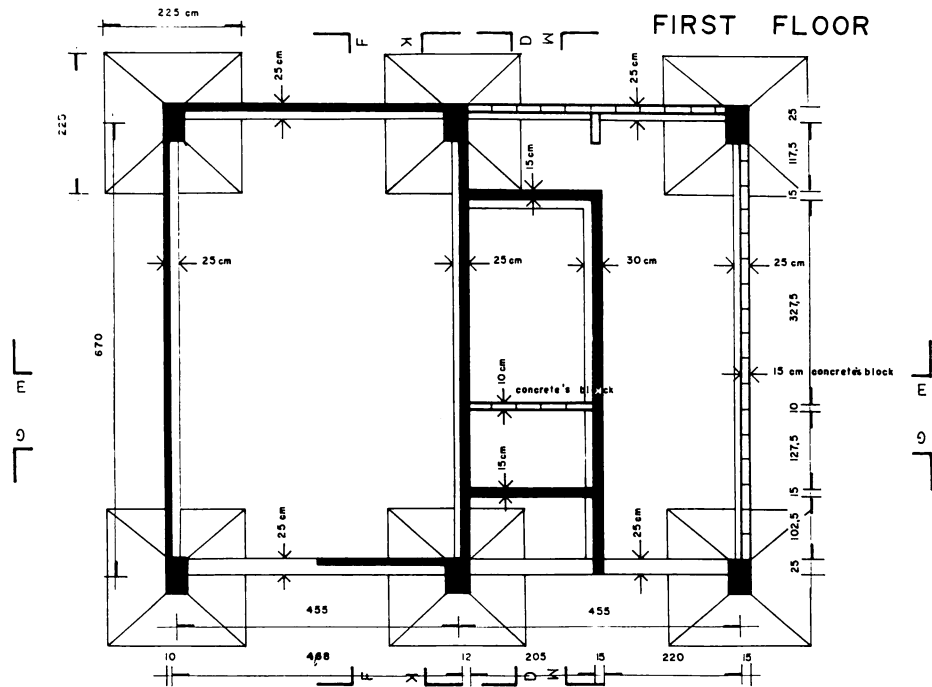


Fig. 1 First floor and basement

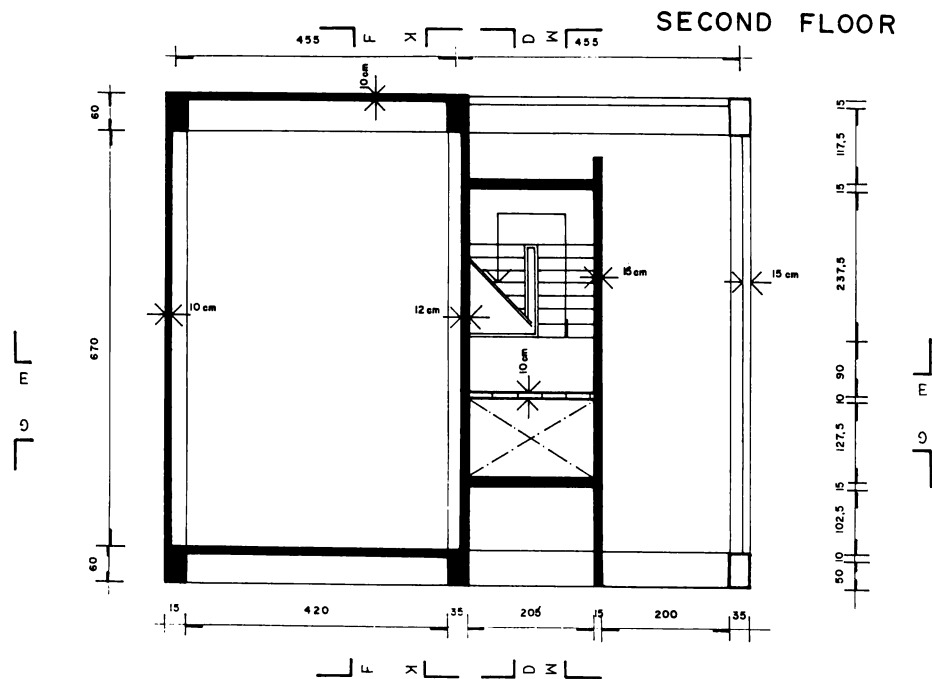


Fig. 2 Second floor plan

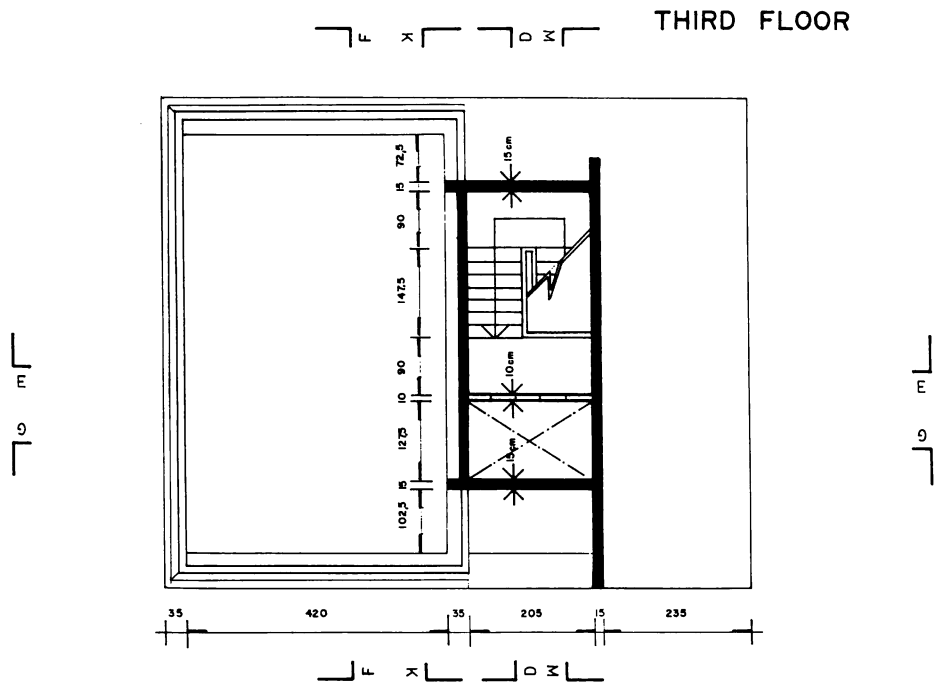


Fig. 3 Third floor plan

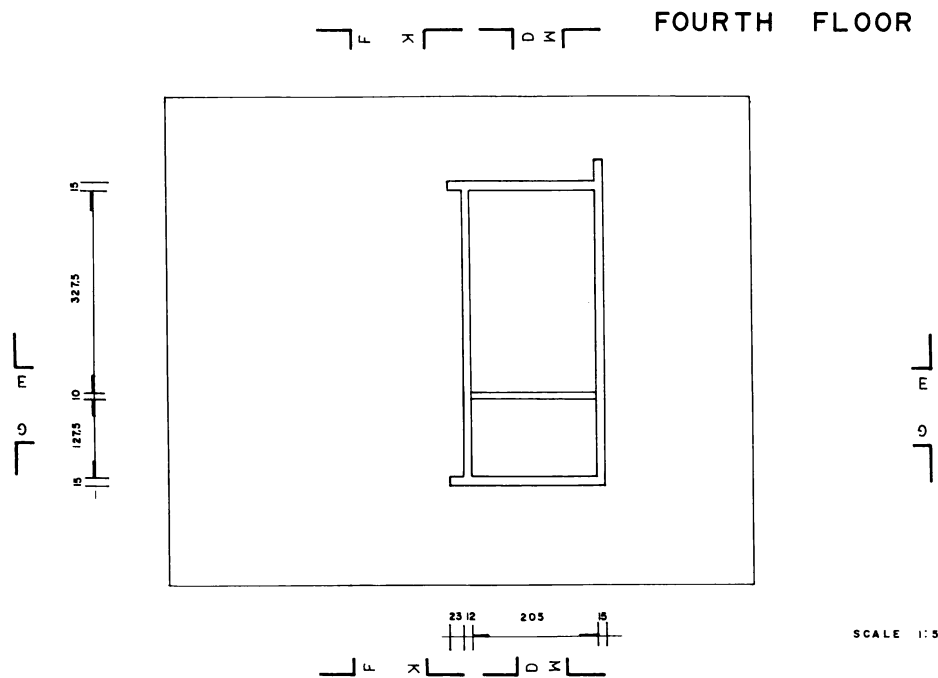


Fig. 4 Fourth floor plan

SCALE 1:30

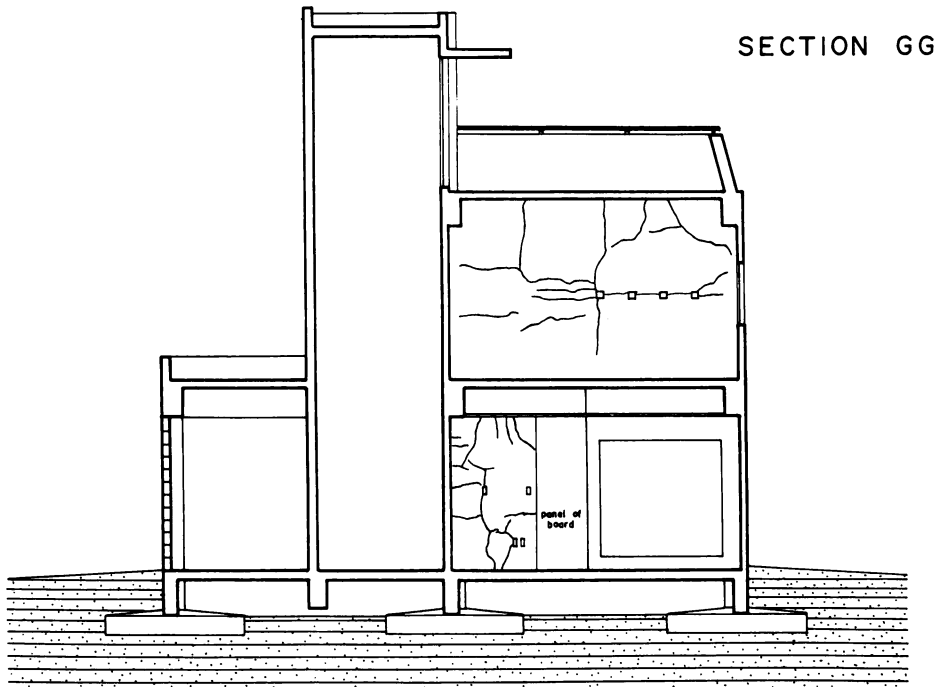


Fig. 5 Crak pattern in north wall

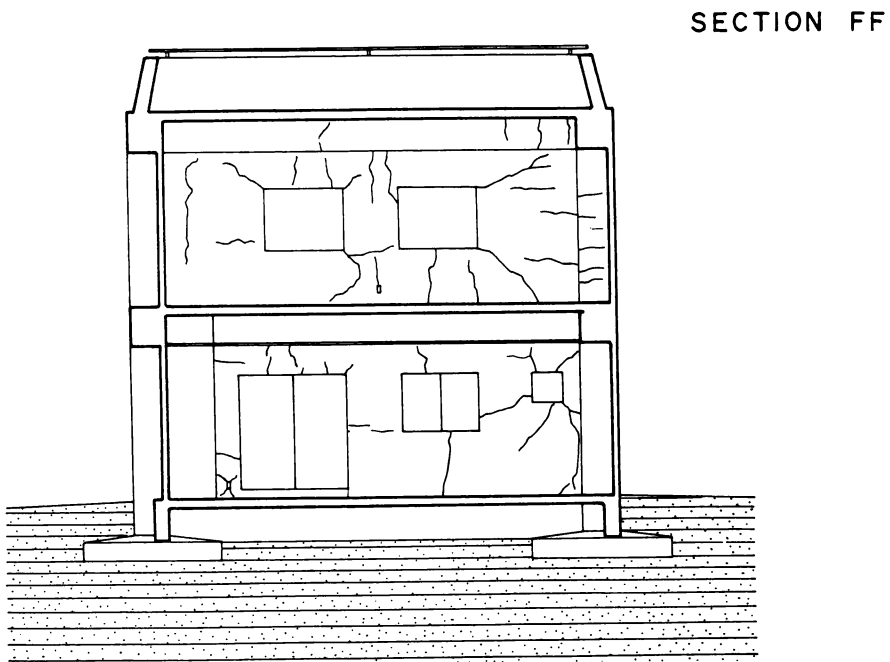


Fig. 6 Crak pattern in east wall

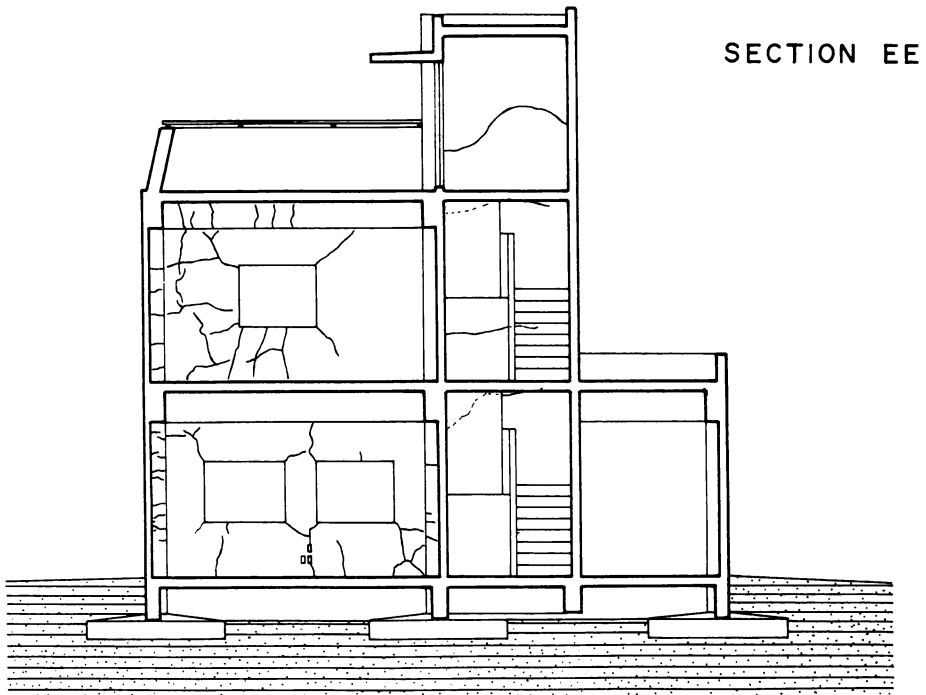


Fig. 7 Crak pattern in south wall

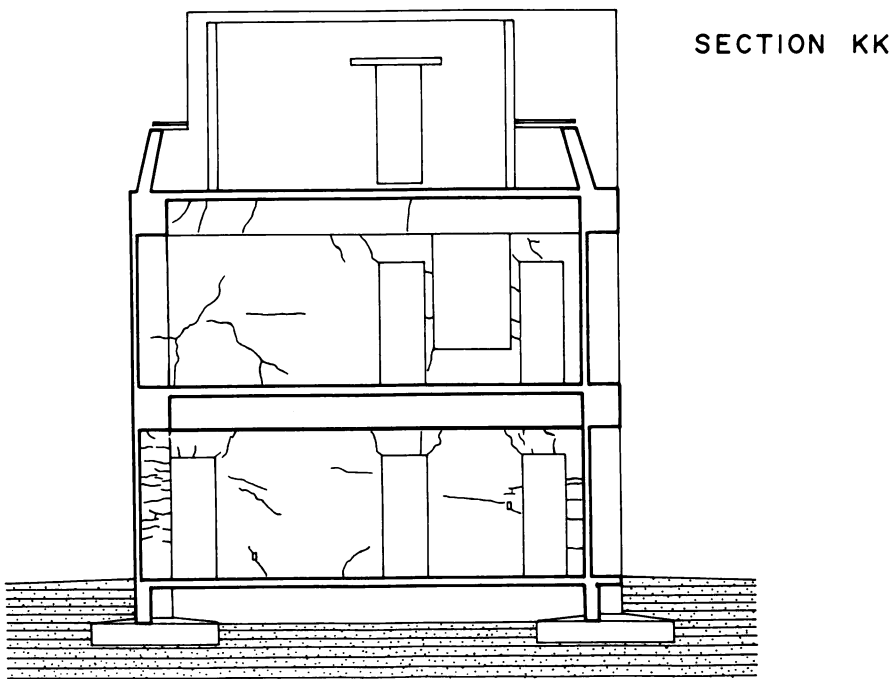


Fig. 8 Crak pattern in north wall

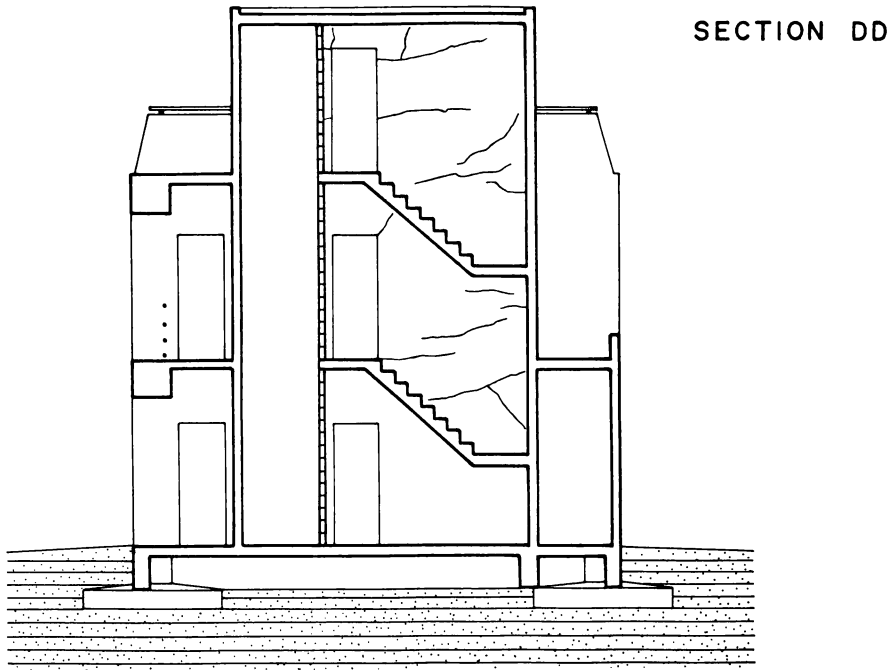


Fig. 9 Crak pattern in interior wall

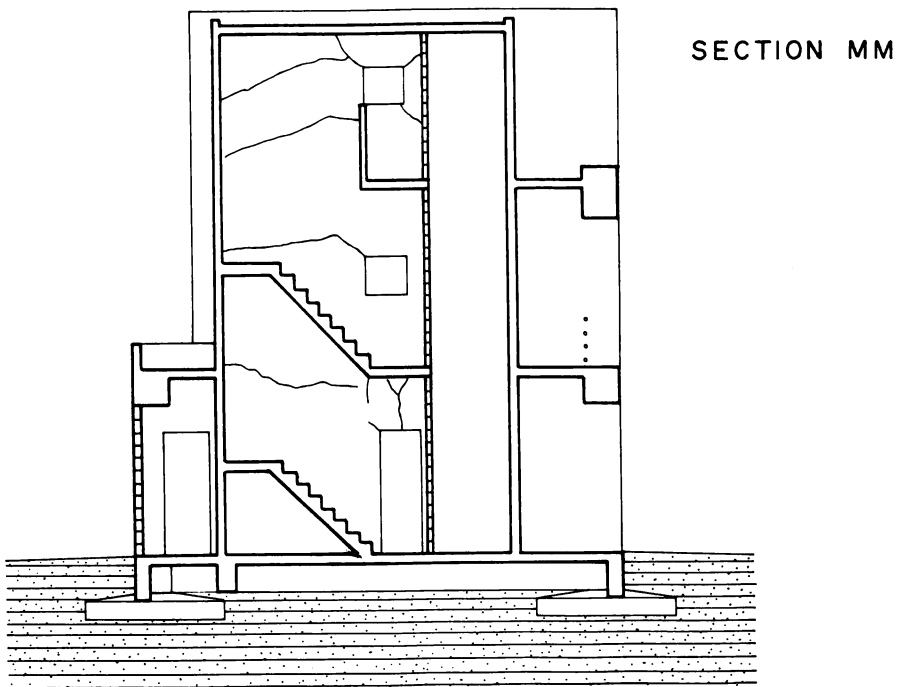


Fig. 10 Crak pattern in interior wall

I –(a) **THICKNESS OF THE SLAB**

According to AIJ, the minimum value of slab thickness is shown in the next table:

Table 1. Required thickness by AIJ

Support Conditions	Slab thickness t (cm)
All edges fixed	$t = 0.02 \left( \frac{\lambda - 0.7}{\lambda - 0.6} \right) \left( 1 + \frac{W_p}{1000} + \frac{I_x}{1000} \right) I_x$
Cantilever	$t = \frac{I_x}{10}$

being in this case:

$$\lambda = l_y / l_x = 1.59$$

$$l_x = \text{effective span length in the short direction} = 420 \text{ cm}$$

$$l_y = \text{effective span length in the long direction} = 670 \text{ cm}$$

$$W_p = \text{sum of live load and weight of finishing (kg/m}^2\text{)} = 372.7 \text{ kg/m}^2 \text{ (see Table 3)}$$

For the study of Slab 1 of second floor, corresponds to apply the first case of Table 1, it is:

$$t = 0.02 \left( \frac{1.59 - 0.7}{1.59 - 0.6} \right) \left( 1 + \frac{372.7}{1000} + \frac{420}{1000} \right) \times 420 = 13.5 \text{ cm}$$

The real thickness of slab is 15 cm, which means that for AIJ, it is appropriate for the assumed load.

The thickness of slabs, according to DIN is defined by a simplified verification of the slenderness to flexion.

The limit of slenderness  $l_i/h$  of elements submitted to flexion, can not be larger than the value 35,

$$l_i/h \leq \text{or} = 35$$

$$\rho = \text{short span length of slab.}$$

$$\alpha = l_i/l \text{ coefficient that depends on the kind of supports system (To see Table 2)}$$

$$h = t, \text{ thickness of slab}$$

$$35 = \text{number fixed by the standard}$$

When the slab support the walls loads directly, the slenderness must be:

$$l_i/h \leq \text{or} = 150/l_i$$

$$150 = \text{number fixed by the standard}$$

$$l_i = \alpha \times l, \text{ for bent elements whose deflections are mainly originated by the acting load on the span.}$$

For the case in study, it is:

$$l = 4.20 \text{ m} \quad l_i/h = 4.2/0.15 = 28$$

$$\alpha = 1 \text{ (see point c)}$$

$$l_i/h \leq \text{or} = 35$$

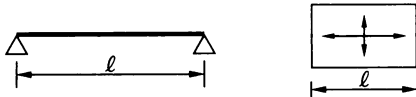
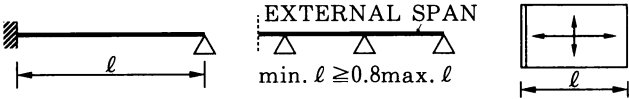
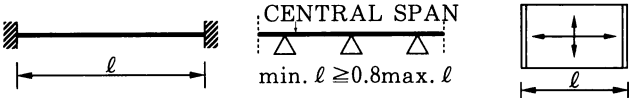
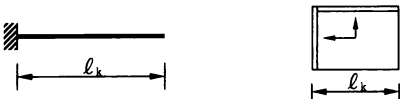
$$4.20/0.15 \leq 35, \text{ then } 4.20/35 \leq 0.15$$

$$28 \leq 35 \quad 0.12 \leq 0.15$$

The application of DIN standard reveals that the thickness of the slab S1 is appropriate.



Table 2. Values  $\alpha$  for different support systems.

	1	2
	STATIC SYSTEM	
		$\alpha = l_i / l$
1		1.00
2	 <p style="text-align: center;">EXTERNAL SPAN min. <math>l \geq 0.8 \text{max. } l</math></p>	0.80
3	 <p style="text-align: center;">CENTRAL SPAN min. <math>l \geq 0.8 \text{max. } l</math></p>	0.60
4		2.40

**I –(b) DETERMINATION OF REQUIRED AREAS OF STEEL AND MAXIMUM MOMENTS OF THE SLAB**

According to AIJ:

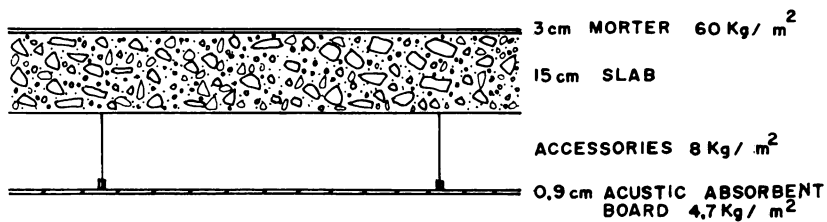


Fig. 11 Detail of slab and finishing

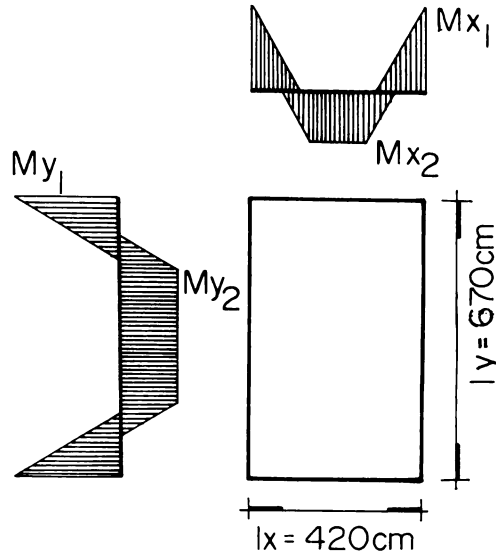


Fig. 12 Moment diagrams of Slab 1

In the slab S1 of second floor, the values of moments are:

$$W = \text{Total uniform load per unit area} = 732.2 \text{ kg}$$

$$W_x = \frac{l_x^4}{l_x^4 + l_y^4} \times W = \frac{6.7}{6.7+4.2} \times 732.2 = 634.36 \text{ kg}$$

$$M_{x_1} = -\frac{1}{12} \times W_x l_x^2 = -\frac{1}{12} \times 634.36 \times 4.2 = -932.5 \text{ kg m/m}$$

$$M = \frac{1}{18} \times W_x l_x^2 = \frac{1}{18} \times 634.36 \times 4.2 = +621.6 \text{ kg m/m}$$

$$M = -\frac{1}{24} \times W_x l_x^2 = -\frac{1}{24} \times 732.2 \times 4.2 = -538.1 \text{ kg m/m}$$

$$M = \frac{1}{36} \times W_x l_x^2 = \frac{1}{36} \times 732.2 \times 4.2 = +358.1 \text{ kg m/m}$$

Consequently in the direction xx, the bars of steel are designed in function of  $-932.5 \text{ kg m/m}$ , and in the direction yy according to  $-538.1 \text{ kg m/m}$ .

$$M = a_t \times f_t \times j \quad a_t = \frac{M}{f_t \times j}$$

$a_t$  = sectional area of tensile stress of reinforcing bars.

$f$  = allowable unit tensile stress of reinforcing bars =  $2000 \text{ kg/cm}^2$

(in case of long term loads)

$$j = 7/8 d$$

$$\text{In the direction xx, } a_t = \frac{93250}{2000 \times 10.93} = 4.26 \text{ cm}^2/\text{m}$$

$$a_t = \frac{a_{D10} + a_{D13}}{2} \times 5 = \frac{0.71 + 1.27}{2} \times 5 = 4.95 \text{ cm}^2$$

$$\text{In the direction yy, } a_t = \frac{M}{f_t \times j} = \frac{53816}{2000 \times 10.93} = 2.46 \text{ cm}^2/\text{m}$$

$$a_t = 4 \times 0.71 \text{ cm}^2 = 2.85 \text{ cm}^2 = 4 \text{ bars D10/m}$$

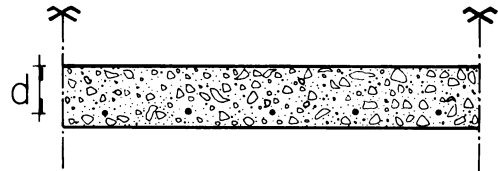


Fig. 13 Effective depth of slab

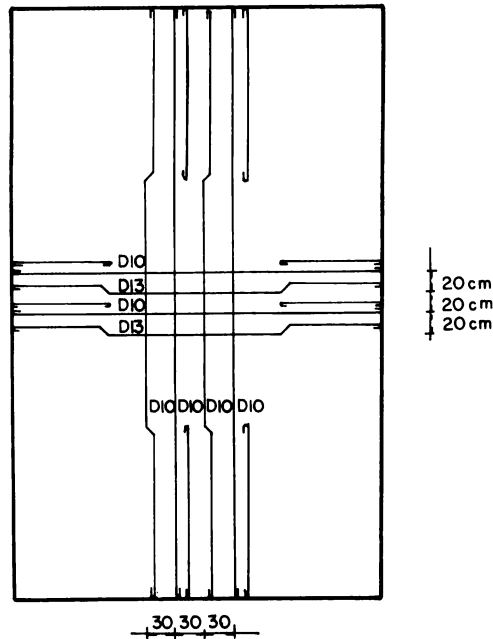


Fig. 14 Arrangement of reinforcing bars of Slab 1

The AIJ standard defines two possible values of yield moment, which for the direction  $xx$  are:

$$\begin{aligned} \text{a) - } M_{y_{.xx}} &= a_{t_{.xx}} \times \sigma_y \times j && \text{being: } a_t = \text{sectional area of tensile reinforcing bars.} \\ M_{y_{.yy}} &= a_{t_{.yy}} \times \sigma_y \times j && \sigma_y = 3000 \text{ kg/cm}^2 \\ &&& j = 7/8 d = 7/8 \times 12.5 \text{ cm} = 10.93 \text{ cm} \\ M_{y_{.xx}} &= 4.95 \times 3000 \times 10.93 = 162310.5 \text{ kgcm/m} = 1623 \text{ kgm/m} \\ 1623 \text{ kgm/m} &> 932.5 \text{ kgm/m} \end{aligned}$$

For the direction  $yy$  the value are:

$$\begin{aligned} M_{y_{.yy}} &= a_{t_{.yy}} \times \sigma_y \times j = 2.85 \times 3000 \times 10.93 = 93451.5 \text{ kgcm/m} = 934.5 \text{ kgm/m.} \\ 934.5 \text{ kgm/m} &> -538.1 \text{ kgm/m} \end{aligned}$$

$$\text{b) - } M_{y_{.xx}} = a_{t_{.yy}} \times \sigma_y \times j \quad \text{and} \quad M_{y_{.yy}} = a_{t_{.yy}} \times \sigma_y \times j$$

In this case only the value of  $j$  changes, it is,  $d \times 0.9 = 12.5 \times 0.9 = 11.25 \text{ cm}$

$$\begin{aligned} M_{y_{.xx}} &= 4.95 \text{ cm} \times 3000 \times 11.25 = 167062.5 \text{ kgcm} = 1670.6 \text{ kgm} \\ 1670.6 \text{ kgm} &> 932.5 \text{ kgm} \\ M_{y_{.yy}} &= 2.85 \text{ cm} \times 3000 \times 11.25 = 96187.5 \text{ kgcm} = 961.87 \text{ kgm} \\ 961 \text{ kgm/m} &> 538.1 \text{ kgm/m} \end{aligned}$$

When the end moment is equal to the yield moment  $M_{y_{.xx}}$ , then

$$M_{y_{.xx}} = 1623.1 \text{ kgm/m} = \frac{W_1 \times \ell^2}{12} \quad \text{and therefore:}$$

$$W_1 = \frac{1623.1 \text{ kg} \times 12}{4.2^2} = 1104.1 \text{ kg/m} \quad Mc = \left( \frac{1}{8} - \frac{1}{12} \right) \times W_1 \times \ell^2 = \frac{1}{24} \times 1104.1 \times 4.2^2 = 811.5 \text{ kgm}$$

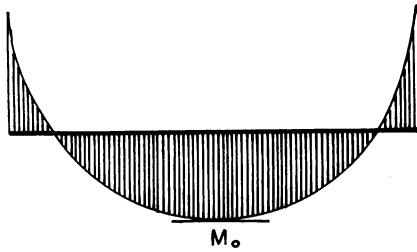


Fig. 15 Bending moment diagram when end moments reach yield moment

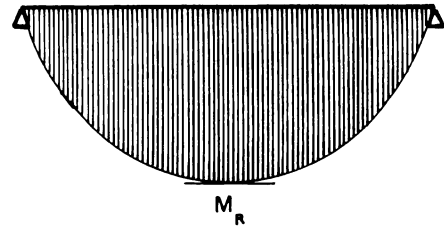


Fig. 16 Bending moment diagram when the moment of central part reaches the resistant moment

When the end moments reaches the value of yield moment, the section of end gyrates freely. When the condition of central part become in yield hinges:

$$M_y - M_c = M_R = 1623.1 \text{ kg m} - 811.5 \text{ kg m} = 811.5 \text{ kg m}$$

$$M_R = \frac{W_2 \times \ell^2}{8} = 811.56 \text{ kg m} \quad W_2 = \frac{811.5 \text{ kg} \times 8}{4.2} = 368.0 \text{ kg}$$

$$W_1 + W_2 = \text{RTL} = \text{Resistant total load.}$$

When the slab reaches this value :  $1104.14 \text{ kg} + 368.05 \text{ kg} = 1472.19 \text{ kg}$ , neither the end props nor the central part can support the slab. Consequently, the slab would fall down if its load is equal or larger than  $1472.19 \text{ kg}$ .

But if the arch action of the slab is considered, it is possible to obtain a bigger value than the above result, for the fall down of the slab.

### MAXIMUM MOMENTS AND DETERMINATION OF REQUIRED AREAS OF STEEL BARS, ACCORDING TO METHOD DIN

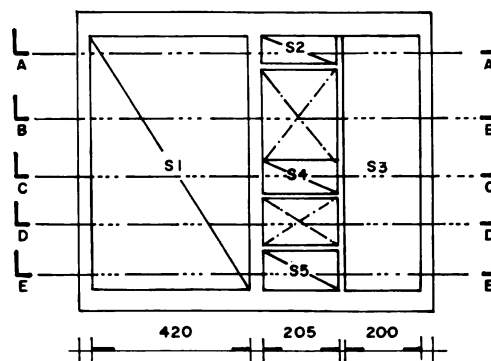


Fig. 17 Continuity and discontinuity conditions of Slab 1

In accordance with the method used in Uruguay (method taught in the Faculty of Architecture) for the determination of moments, the Slab 1 would have three different reinforcements according the direction  $xx$ . The different reinforcements depend on the conditions of continuity with or without the neighboring slabs, which determine the values of the moments of Slab 1.

From the above, here is studied only the sections which determine the bigger moments of the slab. Those are the sections AA and CC, in which the end moments and span moments are equal.

Calculation of Moments of Sections AA and CC:

The moments of the slab are calculated according which is established in the Table 3, and according to the Table made by Marcus for two way solid flat slabs and two-way waffle flat slabs. The Table of Marcus determines the values of  $\kappa_x$ ,  $\kappa_y$ ,  $\nu_x$  and  $\nu_y$ .

Table 3 Determination of bending moment values for different support systems

span moments	$M_o = \frac{q \times l}{1422}$ $M_c = M_o \times \nu_x$ 	$M_o = \frac{q \times l}{8}$ $M_c = M_o \times \nu_x$ 	$M_o = \frac{q \times l}{24}$ $M_c = M_o \times \nu_x$ 
	support moments	$M = \frac{q \times l}{8}$ $M_s = M - Rb/4$	$M = \frac{q \times l}{12}$ $M = M - Rb/4$

SLAB 1

$q = 732.2 \text{ kg}$      $l_y/l_x = 1.59$      $\kappa_x = 0.939$      $\kappa_y = 0.061$   
 $q_x = \kappa_x \times q = 732.7 \times 0.939 = 688 \text{ kg}$      $q_y = \kappa_y \times q = 732.2 \times 0.061 = 45 \text{ kg}$

SLAB 2

As the rate  $l_y/l_x = 2.82$  the whole load of S2 is carried to the longer sides only, which means that the Slab 2 does not affect to the Slab 1.

SLAB 3

$l_y/l_x = 3.35$     and     $q_y = 632.7 \text{ kg}$   
 The Slab 1 has  $\lambda = 1.59$      $\nu_x = 0.825$

The span moment =  $\frac{q \times l^2}{14.22} = \frac{688 \times 4.2^2}{14.22} = 853.4 \text{ kg}$

$M_x = M_o \times \nu_x = 854 \times 0.825 = 704.5 \text{ kg m/m}$

End moment =  $\frac{q \times l^2}{8} - \frac{R \times b}{4} = \frac{688 \times 4.2^2}{8} - \frac{1445 \times 0.35}{4}$   
 $= 1391 \text{ kg m/m}$

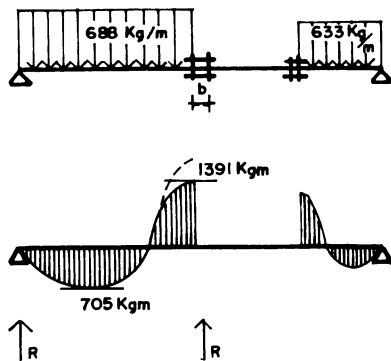
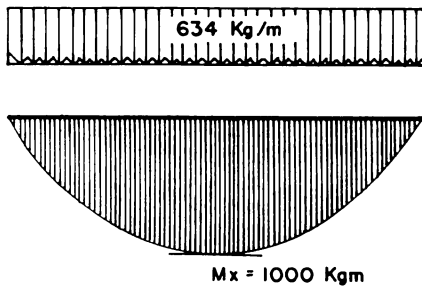


Fig. 18 Bending moment diagram with respect to sections AA and CC (see Fig.17)

Calculation of Moments of Sections BB and DD

For these sections, the slab 1 does not have continuity, therefore:

$\kappa_x = 0.865$      $q_x = 732.2 \text{ kg} \times 0.865 = 634 \text{ kg/m}$



$$M_{x_0} = \frac{q_x \times \ell^2}{8} = \frac{634 \text{ kg} \times 4.2^2}{8}$$

$$M_{x_0} = 1397.9 \text{ kgm/m} \quad M_x = 0.715 \times 1397.9 = 999.5 \text{ kgm/m}$$

$$M_x = \nu_x \times M_{x_0} \quad \nu_x = 0.715$$

$$\text{Then, } F_e \text{ (necessary area of steel)} = \frac{M_u}{Z \times \sigma_{e_u}}$$

Fig. 19 Bending moment diagram according to sections BB and DD

Being :  $M_u = M_x$  multiplied by a coefficient of security  $= M_x \times 1.5$

$Z$  = Internal lever arm, that varies between  $0.83 \times h$  and  $0.92 \times h$ , conforms to:

- 1) - the degree of requirement of concrete in the compression zone,
- 2) - deformation of the steel  $\epsilon_s = 5\%$
- 3) -  $\bar{\mu} < 0.3$ , being  $\bar{\mu} = \frac{F_e}{b \times H} \times \frac{\beta_s}{\beta_R}$  (Yield Strength)  
(Characteristic strength of concrete)

According to the practice of decades  $Z = \frac{7}{8} \times d$  is used.

In this case the value of  $3000 \text{ kg/cm}^2$  is used for the building, but using the formula correspondent to DIN.

$$F_e = \frac{1391 \times 1.5}{10.93 \text{ cm} \times 3000 \text{ kg/cm}^2} = \frac{208650 \text{ kgcm/m}}{32790 \text{ kgcm/cm}^2} = 6.36 \text{ cm}^2/\text{m}$$

The areas of reinforcements are determined from the above, whenever compression reinforcements do not exist.

The area of steel obtained by the method DIN is bigger than that obtained by AIJ. That is due to the larger value of the bending moment correspondent to the direction  $xx$ , and in despite of the bigger yield strength value used in this formula [ $3000 \text{ kg/cm}^2$  (DIN)  $>$   $2000 \text{ kg/cm}^2$  (AIJ)]. The determined area of steel in the direction  $xx$  is  $6.36 \text{ cm}^2$ , therefore one possible arrangement for the steel bars is:

$$a_s = \frac{a_{D10} + a_{D13}}{2} \times 7 = \frac{0.713 + 1.27}{2} \times 7 = 6.94 \text{ (cm)}$$

In the direction  $yy$   $\kappa_y = 0.061$   $q_y = 732.2 \times 0.061 = 45 \text{ kg/m}$

$$M = \frac{q_y \times \ell_y^2}{8} = \frac{45 \times 6.7^2}{8} = 253 \text{ kgm/m}$$

$$M_{c_{yy}} = M_o \times \nu_y = 253 \times 0.715 = 181 \text{ kgm/m}$$

$$F_e = \frac{181 \times 1.5}{10.93 \times 3000} = 0.82 \text{ cm}^2$$

#### I -(c)- REAL FIBER TENSILE STRESS AND ITS COMPARISON WITH THE $\sigma_{ct}$ (ALLOWABLE TENSILE STRESS of CONCRETE)

According to AIJ STANDARD:

$$\sigma_t \text{ (Real Fiber Tensile Stress)} = M/z$$

$M$  : Bending moment of de Section

$$z \text{ (Section Modulus)} = \frac{b \times t^2}{6} = \frac{I_x}{t/2} = \frac{100 \times 15}{6} = 3750 \text{ (cm}^3\text{)}$$

$$M_{x_1} = -1/12 \times W_x \times \ell_x^2 = -932.5 \text{ kg m/m}$$

$$M_{x_2} = 1/18 \times W_x \times \ell_x^2 = +621.6 \text{ kg m/m}$$

$$M_{y_1} = -1/24 \times W \times \ell_x^2 = -538.1 \text{ kg m/m}$$

$$M_{y_2} = 1/36 \times W \times \ell_x^2 = +358 \text{ kg m/m}$$

(For the determination of  $w$  and  $w_x$ , to see Consideration B- on the slab)

$$\sigma_{x_1} = -93250/3750 = 24.8 \text{ (kg/cm}^2\text{)}$$

$$\sigma_{x_2} = +62167/3750 = 16.5 \text{ (kg/cm}^2\text{)}$$

$$\sigma_{y_1} = -53816/3750 = 14.3 \text{ (kg/cm}^2\text{)}$$

$$\sigma_{y_2} = +35800/3750 = 9.5 \text{ (kg/cm}^2\text{)}$$

$$cf_1 = F_c/10 = \frac{210}{10} = 21 \text{ (kg/cm}^2\text{)} ; F_c/20 = \frac{210}{20} = 10.5 \text{ (kg/cm}^2\text{)}$$

According to the AIJ standard, the allowable tensile stress of concrete is defined in function of design standard strength of concrete ( $F_c$ ), defining two values:

- 1)  $F_c/10$ , being  $F_c = 210 \text{ kg/cm}^2$  ;  $210 \text{ kg/cm}^2 / 10 = 21 \text{ kg/cm}^2$ , if the value of the fiber tensile stress is lesser than  $F_c/10$ , the cracking of the concrete might not occur.
- 2)  $F_c/20 = 210 \text{ kg/cm}^2 / 20 = 10.5 \text{ kg/cm}^2$ , from which if the value of real tensile stress of top fiber is equal or bigger than it, the cracking of the concrete occurs inexorably.

From the above, it is possible to say that cracks appear in the top surface of slab in both directions (xx and yy) close and along the supports, since:  $24.8 \text{ kg/cm}^2 > 210 \text{ kg/cm}^2 / 20$ , this is  $24.8 \text{ kg/cm}^2 > 10.5 \text{ kg/cm}^2$  and  $14.3 \text{ kg/cm}^2 > 210 \text{ kg/cm}^2 / 20$ , this is  $14.3 \text{ kg/cm}^2 > 10.5 \text{ kg/cm}^2$ .

And it is assumed that in the bottom side of the slab occurs a crack pattern parallel to the long sides and located in the central part of slab, even if it was not possible to prove, owing to the presence of the ceiling and its frame.

### I –(c) COMPARISON BETWEEN CALCULATED FIBER TENSILE STRESS AND THE THE ALLOWABLE TENSILE STRESSES OF CONCRETE ACCORDING TO THE DIN STANDARD

The principal difference between the standard DIN and the standard AIJ with respect to this aspect, lain in how is defined the numerical value of tensile strength of concrete.

The tensile strength of concrete depends on many factors, above all, on the adherence between the aggregates and the mortar.

The values of assays are very dispersed, whereas the stress due to temperature and due to the shrinkage, for example, can not be avoided.

According to the method of assay, the DIN distinguishes:

- 1) - Axial Tensile Strength
- 2) - Splitting Tensile Strength
- 3) - Bending Tensile Strength, Modules of Rupture ( $\beta_{Bz}$ )

In this study, the third must be applied, since the slab is submitted to bending tensile strength:

$$\beta_{Bz} = Mu/w$$

Being:  $Mu$  = Moment of the section multiplied by a coefficient of security.

$w$  = Section Modulus (defined by  $z$ , according to AIJ)

With respect to the numerical value of Bending Tensile Strength =  $\beta_{Bz}$

$$\beta_{Bz} = 2.5 \sqrt[2]{\beta_w} \quad \text{or} \quad 1.0 \sqrt[3]{\beta_w^2}$$

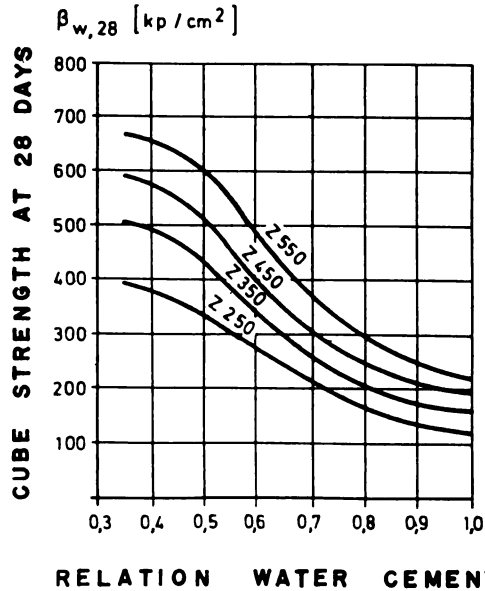


Fig. 20 Influence of factor W/C on the strength to the compression of concrete  $\beta_{w28}$ , for cements of several patternized strength

$\beta_w$  = Compressive cube strength of concrete at 28 days, value that depends on the type of used cement (z), and on the factor w/c (relation: water/cement).

For example if the concrete of 250 kg/cm<sup>2</sup> of smallest resistance to compression at 28 days, is taken:

$$\beta_{Bz} = 2.5 \sqrt{\beta_w} \quad 2.5 \sqrt{250 \text{ kg/cm}^2} = 39.5 \text{ kg/cm}^2$$

Thus, from the initial value 39.5 kg/cm<sup>2</sup> is defined a range of allow ability of +25%:

$$39.5 \text{ (kg/cm}^2) \times 0.75 = 29.6 \text{ (kg/cm}^2)$$

$$39.5 \text{ (kg/cm}^2) \times 1.25 = 49.4 \text{ (kg/cm}^2)$$

$$29.6 \text{ (kg/cm}^2) < \text{allowable tensile stress values} < 49.4 \text{ (kg/cm}^2)$$

In order to apply this formula to the present study of the slab, the value 210 kg/cm<sup>2</sup> is used (value of cylindrical strength to compression of this building).

This value comes from a cylindrical sample, while  $\beta_{Bz} = 2.5 \sqrt{\beta_w}$  uses a cubic sample of concrete, accordingly, it is necessary to do the correspondent settlements:

For the calculation of compressive cylindrical resistance  $\beta_c$ , DIN 1045 standard establishes the following relation:

$$\beta_w = 1.25 \beta_c \quad \text{for concrete's strength} \leq 150 \text{ kg/cm}^2$$

$$\beta_w = 1.18 \beta_c \quad \text{for concrete's strength} \geq 250 \text{ kg/cm}^2$$

and 210 kg/cm<sup>2</sup> corresponds to a cylindrical sample, whereby:

$$\text{as } 210 \text{ kg/cm}^2 \sim 250 \text{ kg/cm}^2 \text{ of a cubic sample: } \beta_{Bz} = 2.5 \sqrt{1.18 \times 210 \text{ kg/cm}^2} = 39.3 \text{ kg/cm}^2$$

form which is defined an interval of allowability:

$$(39.3 - 39.3 \times 0.25) \text{ kg/cm}^2 < \text{interval of allowability} < (39.3 + 39.3 \times 0.25) \text{ kg/cm}^2$$

The value of the biggest moment of the Slab 1, determined by the method used in Uruguay (see consideration B-related with the slab) is 1391 kgm/m, for which:

$$1391 \text{ kgm/m} \times 1.5 = 2086.5 \text{ kgm/m (Maximum moment} \times \text{coefficient of security)}$$



The biggest fiber tensile stress is:  $208650 \text{ kg.cm} / 3750 \text{ cm}^2 = 55.64 \text{ kg/cm}^2$

The above value means that the biggest real fiber tensile stress is not within the range of allow ability, according to this standard DIN.

If the second numerical value of bending tensile strength is applied:

$$\beta_{Bz} = \sqrt[3]{\beta_w^2} = \sqrt[3]{(1.18 \times 210)^2} = 38.02 \text{ kg/cm}^2$$

$$(38.0 - 38.0 \times 0.25) \text{ kg/cm}^2 < \text{range of allowability} < (38 + 38 \times 0.25) \text{ kg/cm}^2$$

$$28.5 \text{ kg/cm}^2 < \quad \quad \quad \quad \quad < 47.52 \text{ kg/cm}^2$$

Neither for this interval, the defined calculated fiber tensile stress is within the range of allowability. And if furthermore the established by DIN 1045 is considered, which defines a “measure of prevention” by the nominal compression stress  $\beta_{wN} = 50 \text{ kg/cm}^2$

$\beta_w$  : compression cube strength of concrete

$\beta_{wN}$ : nominal compression cube strength of concrete

If this value is introduced into the formulæ of  $\beta_{Bz}$ , it becomes:

$$\beta_{wN} = 50 \text{ kg/cm}^2 = 13.2 \text{ kg/cm}^2$$

And the defined range is between  $0.75 \times \sqrt[3]{50 (\text{kg/cm}^2)}$  and  $1.25 \times \sqrt[3]{50 (\text{kg/cm}^2)}$  :

$$9.91 (\text{kg/cm}^2) < \beta_B < 16.5 (\text{kg/cm}^2)$$

If  $\beta_{Bz} = \beta_{wN} \times 2.5 = 50 (\text{kg/cm}^2) \times 2.5 = 125 (\text{kg/cm}^2)$  is taken:

$$125 (\text{kg/cm}^2) \times 0.75 < \text{range of allowability} < 125 (\text{kg/cm}^2) \times 1.25$$

$$93.75 (\text{kg/cm}^2) < \quad \quad \quad \quad \quad < 156.25 (\text{kg/cm}^2)$$

This interval seems more close to that defined by the AIJ:

$$10.5 (\text{kg/cm}^2) < \text{range of allowability} < 21 (\text{kg/cm}^2)$$

The value of fiber tensile stresses correspondent to the end moments is:

$$55.6 (\text{kg/cm}^2) \gg 21 (\text{kg/cm}^2) \quad (\text{in the direction xx, mentioned already})$$

The values of fiber tensile stresses correspondent to central moments are:

$$28.2 \text{ kg/cm}^2 > 21 \text{ kg/cm}^2 \quad (\text{along the direction yy})$$

$$7.24 \text{ kg/cm}^2 \ll 21 \text{ kg/cm}^2 \quad (\text{along the direction xx})$$

The comparison with the obtained values for the fiber tensile strength and those values defined by all the intervals of allowability of standard DIN reveals the possibility of occurring cracks only in two parts: 1)- The top side of slab along the direction yy and 2)- The bottom side along the central part of the slab according the direction xx.

The top side cracks near to the supports along the direction xx are not revealed, owing to:

- 1)- The assumed conditions for the supports along the direction xx, which do not produce moments.
- 2)- The small value of the loads driven to short sides of slab. But, even if fixed conditions are considered for those supports, neither the results obtained would reveal the presence of actual cracks that presents the slab near and along the supports in the direction xx.

#### I –(d) BOND STRESS AND SHEAR STRESS

According to AIJ STANDARD

$$w = \text{Total uniform load per unit length} = 732.2 \text{ kg/m}$$

Therefore accordingly to direction xx, the value of shear force becomes:

$$Q_{\text{max.xx}} = 732.2 \times 4.2 = 1537.6 \text{ kg} \sim 1538 \text{ kg}$$

The bond stress of tensile reinforcing bars in flexural members,  $\tau_a$ , due to shear force is

computed by:

$$\tau_s = \frac{Q}{\psi_j} \leq f_s$$

being:  $\psi$  : sum of perimeters of tensile reinforcing bars

$$\psi = \frac{\psi_{D10} + \psi_{D13}}{2} \times 5 = \frac{3\text{cm} + 4\text{cm}}{2} \times 5 = 17.5 \text{ cm}$$

$j$  = distance from the center of gravity of compression block to centroid of tensile bars in flexural members, which may be assumed as  $(7/8)d$ .

$$\tau_{s, \dots} = \frac{1538}{17.5 \times 10.93} = 8.04 \text{ (kg/cm}^2\text{)} < f_a$$

$f_a$  : allowable unit bond stress of reinforcing bars, which is  $F_c/15$  for deformed bars.

In this case  $F_c = 210 \text{ (kg/cm}^2\text{)}$ , therefore:

$$\tau_s < f_a \sim 8.04 \text{ (kg/cm}^2\text{)} < \frac{210}{15} \text{ (kg/cm}^2\text{)} = 14 \text{ (kg/cm}^2\text{)}$$

The bond stress obtained by the AIJ standard is within the range of allowability.

With respect to shear stress ( $\tau_s$ ), it must accomplish the following:

$$\tau_s < \min (F_c/30, 5 + F_c/100) = \min (7.0, 7.1) = 7 \text{ (kg/cm}^2\text{)}$$

$$\text{of concrete is defined by: } \tau_s = \frac{Q}{b \times j} = \frac{1538}{100 \times 10.93} = 1.4 \text{ (kg/cm}^2\text{)}$$

Then:  $1.4 \text{ (kg/cm}^2\text{)} < 7 \text{ (kg/cm}^2\text{)}$

The obtained value of shear stress of concrete is also within the allowable values required by the standard AIJ.

#### I –(d) BOND STRESS AND SHEAR STRESS ACCORDING TO DIN

The maximum value of shear force of the slab is equal to:

$$\frac{q_x \times \ell}{2} = \frac{688 \text{ kg/m} \times 4.2 \text{ m}}{2} = 1445 \text{ kg (see consideration b) - on the slab)}$$

The DIN defines one average value for the bond stress:

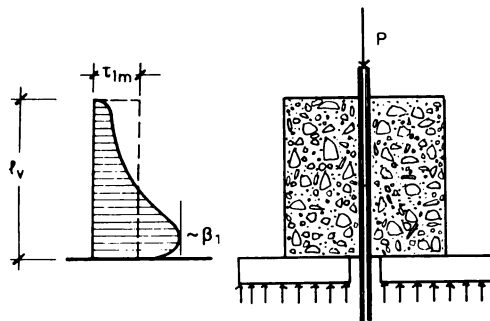


Fig. 21 Experimental condition for determination of bond stress diagram

$$\tau_{lm} = \frac{P}{u \times \ell_v}$$

being: P = Shear force

u = Perimeter of the bar

$\ell_v$  = Length of sector of adherence between the concrete and the steel.

The value of bond stress depends on many factors, they are:

- a- The size and the shape of the sample.
- b- The position of the adherence sector.
- c- The quality of concrete.
- d- The kind of used bars.
- e- The position of the bars during the placing of concrete.

The DIN 1045 defines allowable bond stress  $\tau_1$  for static loads mainly according to the different kind of used concretes.

The allowable bond stresses are shown in the Table 5. (BN- Resistance of patternized cements to compression at 28 days).

Table 4 Allowable valves of bond stresses ( $\tau$ ) for static loads fundamentally (DIN)

	SITUATION DURING THE PLACING OF CONCLETE	$\tau_1$ ALLOWABLE [ kp/cm ]				
		Bn 150	Bn 250	Bn 350	Bn 450	Bn 550
SIMPLE BARS	A	3	3.5	4	4.5	5
	B	6	7	8	9	10
DEFORMED BARS	A	7	9	11	13	15
	B	14	18	22	26	30

Situation A- For all the bars which are not included in the situation B (conditions of unfavorable adherence).

Situation B- For all those bars that have an inclination between 45 and 90 in relation with respect to the horizontal during the placing of concrete; for inclinations lower and for horizontal bars-only if the bars are in the half inferior of the piece when the concrete is placed; or, at least 30 cm under the superior surface of section, or if it is one joint placing of concrete. (good conditions of adherence).

The conditions established in the situation B were considered by AIJ from DIN standard.

For loads fundamentally dynamic, the allowable values are 85 % of those given already.

If it is considered the resistance for the concrete of 210kg/cm<sup>2</sup> (according to AIJ), value that corresponds to cylindric sample one, it is almost equal to that of 250kg/cm<sup>2</sup> correspondent to cubic sample one, then:

$$\tau_{lm} = \frac{P}{u \times \ell_v} = \frac{1445}{100 \times 10.93} = 1.32 \text{ kg/cm}^2 < 9 \text{ kg/cm}^2$$

$$u = \frac{\psi_{D10} + \psi_{D18}}{2} \times 7 = \frac{3+4}{2} \times 7 = 24.5 \text{ cm} \quad \ell_v = 100 \text{ cm}$$

Also according to DIN the obtained bond stress is within of the allowable range.

Note that the allowable bond stresses and the real values obtained, are different comparing the



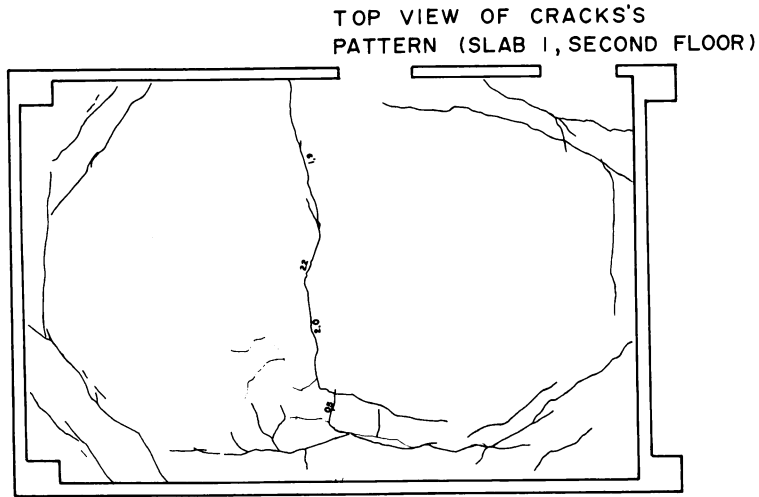


Fig. 22 Crack pattern of Slab 1

top of the slab, near the corners. The above explains the formation of inclined cracks at the corners of the Slab 1, as is shown in the Figure 22.

The crack located in the central part of the slab, along the short direction, occurred due to shrinkage, which is indicated by:

- 1)- Its perpendicular position with respect to the long direction. If the load is big, the direction of the actual crack would be perpendicular to the direction of the actual crack. Whereby the possibility of a big load, as cause of the crack, is neglected here.
- 2)- Its relative location, which is more or less at the middle of the long length of the slab.

**II – ABOUT THE FOUNDATION OF THE BUILDING.**

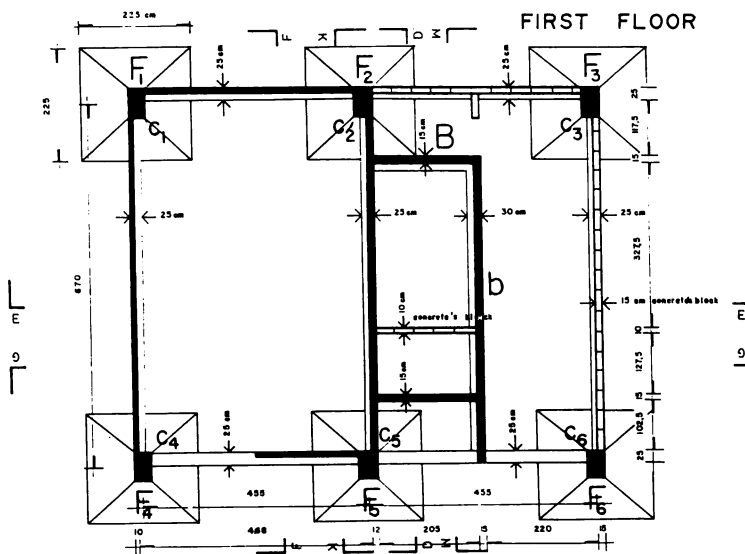


Fig. 23 Foundation plan

The loads of the building are supported by:

- a- Six footings which correspond to the six columns of the building, at one meter of depth from the ground level.
- b- Two beams (B and b of Fig 23) which are supported directly by the soil, at 0.6m of depth the ground level.

The soil of foundation is sand of allowable stress  $f_e$  assumed between  $10T/m^2$  and  $25T/m^2$ . The load resisted by each element of foundation was determined as the summation of loads of several construction elements of the building. Among those elements, the loads of slabs are shown in the next Table.

The values of weight and stress obtained for each footing, are shown in the following Table.

The above Table reveals the possibility of different subsidence among the several footings, since the stress of each footing is different from the others.

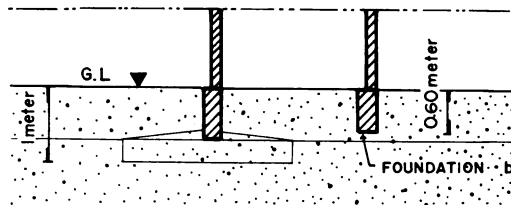


Fig. 24 Depth of footing and foundation beam

Table 5 Total loads of slab

TABLE OF LOADS OF SLABS									
	NUMBER OF SLABS	SLAB	THICKNESS	WEIGHT / M <sup>2</sup>	FINISHING			LIVE LOAD ACCORDING TO FUNCTION	TOTAL WEIGHT / M
					MATERIAL	THICKNESS	WEIGHT/M <sup>2</sup>		
1F	S1	ORDINARY REINFORCED CONCRETE	15 CM	360	MORTER	3 CM	60 Kg	OFFICE = 300Kg / M <sup>2</sup> SHOPPING	724.2 Kg
	S2	"	"	"	MORTER	3 CM	60 Kg	RESIDENCE = 180 Kg / M <sup>2</sup>	600 Kg
	S3	"	"	"	MORTER	3 CM	60 Kg	SHOPPING = 300Kg / M <sup>2</sup>	728 Kg
2F	S1	"	"	"	MOSAIC TILE	4 MM	8 Kg	OFFICE = 300Kg / M <sup>2</sup>	732.7 Kg
	S2	"	"	"	MORTER	3 CM	60 Kg	RESIDENCE = 180 Kg / M <sup>2</sup>	614.7 Kg
	S3	"	"	"	"	"	82.7 Kg	RESIDENCE = 180 Kg / M <sup>2</sup>	614.7 Kg
	S4	"	"	"	MORTER	3 CM	60 Kg	OFFICE = 180 Kg / M <sup>2</sup>	600 Kg
	S5	"	"	"	MORTER	3 CM	60 Kg	ROOF = 180 Kg / M <sup>2</sup>	614.7 Kg
3F	S1	"	"	"	ACUSTIC ABS. BOARD	0.9 CM	4.7 Kg	ROOF = 180 Kg / M <sup>2</sup>	614.7 Kg
	S2	"	"	"	MORTER	3 CM	60 Kg	RESIDENCE = 180 Kg / M <sup>2</sup>	600 Kg
	S3	"	"	"	MORTER	3 CM	60 Kg	ROOF = 180 Kg / M <sup>2</sup>	610 Kg
4F	S1 S2	"	"	"	MORTER	3 CM	60 Kg	ROOF = 180 Kg / M <sup>2</sup>	610 Kg
					WATER PROOFING	0.9 CM	10 Kg		
STAIRS	SA-SA' SB-SB' SC-SC'	SA SB SC	"	"	MORTER	3 CM	60 Kg	RESIDENCE = 180 Kg / M <sup>2</sup>	904 Kg

Table 6 Loads, areas and stresses of footings and beams foundation

FOOTING	LOAD (P) T	AREA (A) m <sup>2</sup>	STRESS (P/A) T/m <sup>2</sup>
F <sub>1</sub>	37.676	5.06	7.44
F <sub>2</sub>	59967	5.06	11.85
F <sub>3</sub>	16925	5.06	3.34
F <sub>4</sub>	37428	5.06	7.39
F <sub>5</sub>	49543	5.06	9.79
F <sub>6</sub>	12071	5.06	2.38
BEAM			
B	6920	0.35	19.77
b	37611	1.74	21.61

The walls that show significant cracks, are supported for those, and beams of foundation, which produce in the soil the higher stresses.

Beam of foundation b = 21.6 T/m<sup>2</sup>

Beam of foundation B = 19.7 T/m<sup>2</sup>

And if furthermore the following aspects of the case are considered:

- a- The deepest level of foundation is at only one meter under the ground level, which might permit an alteration of the rate of water in the soil of foundation.
- b- The beam B and b support a high wall of reinforced concrete of 15cm thickness.
- c- One of the ends of beam b is very near to the beam located between the columns C2 and C3, but nevertheless the beam b is not supported for that beam.
- d- The possibility that, during the construction, the soil of foundation correspondent to the beams b and B, lost their resistance; considering the necessary excavation related to these beams and neighboring beams, the possibility of differential subsidence of the footings and the beams B, becomes even more clear.

Then the conclusion of this study is that

By subsidence of foundation beams, cracks appeared in some walls as show fig 9 and fig 10.

With respect to the crack patterns observed in the figures 5 and 6, the possibility of subsidence of the foundation is not considered as the fundamental cause of their appearance, considering the location of the walls, and the characteristics of the crack patterns.