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(a) Lower-bound mesh (b) Upper-bound mesh Fig. 2. Typical finite element meshes for a circular tunnel (H/D=3, rough interface).





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Fig. 3. Upper-bound rigid-block mechanisms for a circular tunnel.



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(a) Rigid-block mechanism (b) Power dissipation (c) Deformed mesh (d) Plastic multiplier field Fig. 4. Comparison of rigid-block mechanism with finite element limit analysis  $(H/D=1, \phi'=5^{\circ}, \gamma D/c'=1, \text{ smooth interface}).$ 



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